

1. Graph each of the following conic section: $\frac{25(x+2)^2}{225} + \frac{9(y-1)^2}{225} = 1$

Identify all key characteristics such as center, vertex, focus(foci), directrix, major axis, minor axis, and equations of asymptotes

V. Ellipse $\epsilon^2 = a^2 - b^2$

$$\frac{(x+2)^2}{25} + \frac{(y-1)^2}{9} = 1$$

Center: $(-2, 1)$

Vertices: $(-2, 6)$
 $(-2, -4)$

CVertices: $(1, 1)$
 $(-5, 1)$

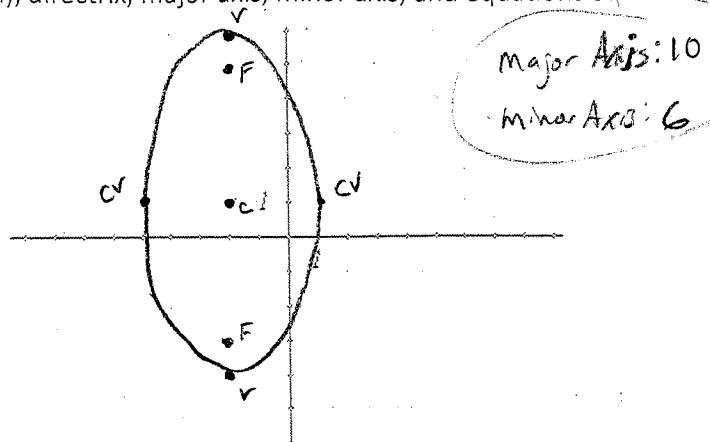
Foci: $(-2, 5)$
 $(-2, -3)$

$a = 5$
 $b = 3$
 $c = 4$

$$c^2 = 5^2 - 3^2$$

$$25 - 9$$

$$r^2 = 16 \quad c^2 = 16$$



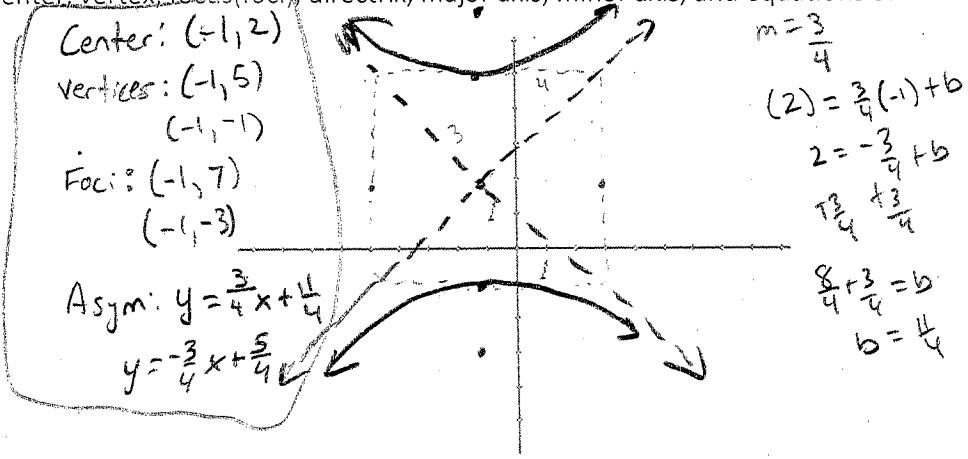
2. Graph each of the following conic sections: $\frac{(y-2)^2}{9} - \frac{(x+1)^2}{16} = 1$ V. Hyp.

Identify all key characteristics such as center, vertex, focus(foci), directrix, major axis, minor axis, and equations of asymptotes where applicable.

$a = 3$
 $b = 4$
 $c = 5$

$c^2 = 3^2 + 4^2$
 $c^2 = 9 + 16$
 $c^2 = 25$
 $c = 5$

$m = -\frac{3}{4}$
 $2 = -\frac{3}{4}(-1) + b$
 $2 = \frac{3}{4} + b$
 $b = \frac{5}{4}$



3. Graph each of the following conic sections: $(y+3)^2 = 12(x+1)$

H. Parabola

Identify all key characteristics such as center, vertex, focus(foci), directrix, major axis, minor axis, and equations of asymptotes where applicable.

vertex $(-1, -3)$

$P = 3$

Focus: $(2, -3)$

Directrix: $x = -4$

Plug 2 in for x solve for y

$$(y+3)^2 = 12(x+1)$$

$$4P = 12$$

$$P = 3$$

$$(y+3)^2 = 12(2+1)$$

$$(y+3)^2 = 12(3)$$

$$(y+3)^2 = 36$$

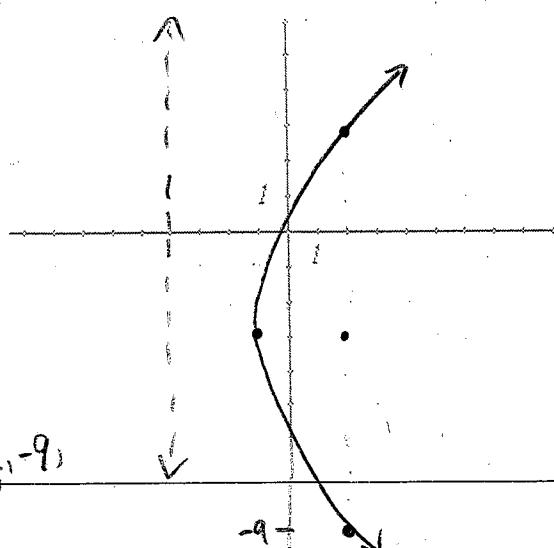
$$(2, -3)$$

$$(2, 9)$$

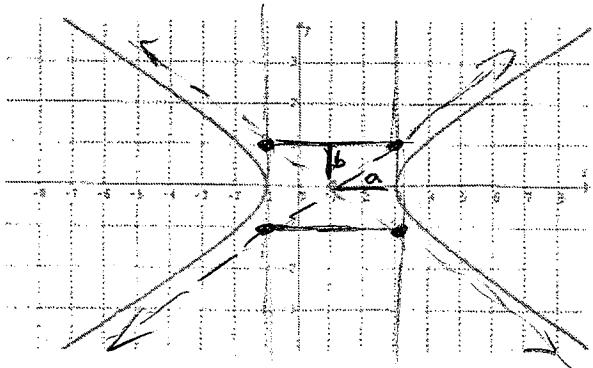
$$(2, -9)$$

$$\frac{y+3}{2} = \pm \frac{6}{3}$$

$$y = 9 \quad y = -3$$



4. Write the equation of the graph below.



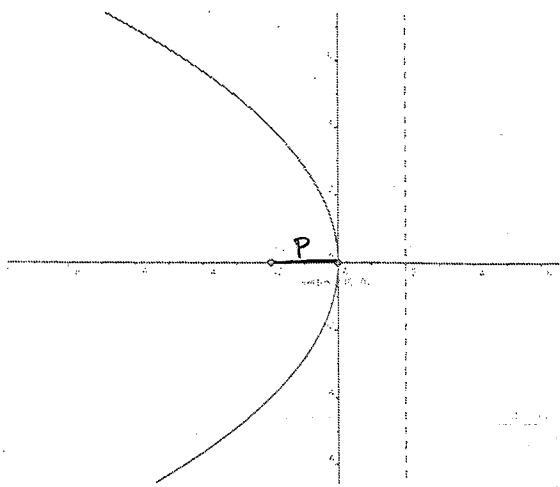
$$a = 2 \quad b = 1$$

$$\frac{x^2}{4} - \frac{y^2}{1} = 1$$

5. Write the equation of the graph below.

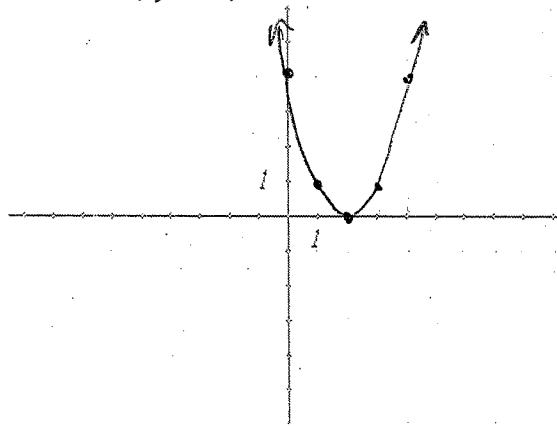
$$P = -2$$

$$y^2 = -8x$$



6. Graph the plane curve described by the parametric equations $x = t + 2$, $y = t^2$, for $-2 \leq t \leq 2$.

t	$x = t + 2$	$y = t^2$	(x, y)
-2	0	4	(0, 4)
-1	1	1	(1, 1)
0	2	0	(2, 0)
1	3	1	(3, 1)
2	4	4	(4, 4)



7. Convert the equation to standard form by completing the square on x and y.

$$4x^2 - y^2 + 32x + 6y + 39 = 0$$

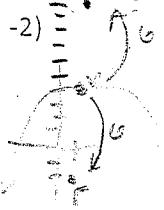
$$4x^2 + 32x - y^2 + 6y = -39$$

$$4(x^2 + 8x + 16) - (y^2 - 6y + 9) = -39 + 64 - 9$$

$$\frac{4(x+4)^2}{16} - \frac{(y-3)^2}{16} = 1$$

$$\frac{(x+4)^2}{4} - \frac{(y-3)^2}{16} = 1$$

8. Find the standard form of the equation of the parabola, given that the vertex is $(1, 4)$ and the focus is $(1, -2)$.



$$x^2 = 4p(y)$$

$$(x-1)^2 = -24(y-4)$$

9. Given the following parametric equation and a value for the parameter t , $x = t^2 + 1$, $y = 4 - t^3$, $t = 2$ find the coordinates of the point on the plane described by the equation corresponding to the t -value.

$$(5, -4)$$